Relevance of Ancient Knowledge to the present century:

De-coding Aryabhatiya Cryptic Numerals, and its application to Modified Tamizh Script to find (1) the number of revolutions of Geo-centric planets in a Mahayuga (43,20,000 Years), comparison of their sidereal periods with their present day values.

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[Note: - This article is prepared using 'Baraha Unicode' software.]

<u>ABOUT THIS ARTICLE</u>: - As a faculty of '*International Academy for Creative Teaching (under Jain Group of Institutions, Bengaluru*)' conducting workshops for Teachers of a few schools in Coimbatore during 2003 – 2009, I faced difficulty in sharing the contributions of Indian mathematicians, specially of Aryabhata-I (5th c. AD) with those teachers (who are not familiar with *Devnagari* Script).

'Tamizh is one of the longest surviving classical languages in the world' and it has been described as the only language of contemporary India which is recognizably continuous with a classical past. The variety and quality of classical Tamil literature has led to its being described as "one of the great classical traditions and literatures of the world". [Ref. Wikipedia]. But, 'Tamizh has fewer scripts than in Devnagari'.

Scripts of any language are *cryptic symbols* for the sounds needed in writing them to communicate with the public.

Tamizh Grantham Scripts are akin to Malayalam scripts, and it is difficult to adapt it to Devnagari'. That is the reason for attempting to this venture.

Modified Tamizh scripts equivalent to Devnagari Scripts (shown within brackets): -

Vowels: உயிரெழுத்து (swara) அ(அ, a), ஆ(आ, A), இ(इ, i), ஈ(ई, I), உ(ʒ, u), ஊ(ऊ, U), [ற(束,Ru)], எ(ए,e), ஏ(ए,E), ஐ(ऐ,ai), ஒ(ओ,o), ஓ(ओ,O), ஔ(ओ,au).

Vyanjana, Consonants: மெய் எழுத்து (वर्गाक्षर)

$$\dot{\mathfrak{G}}=\dot{\mathfrak{G}}$$
 (क्, k), $\dot{\mathfrak{G}}_1$ (ख, K), $\dot{\mathfrak{G}}_2$ (ग, g), $\dot{\mathfrak{G}}_3$ (घ, G), $\dot{\mathfrak{G}}_1$ (इ, ~g)
$$\dot{\mathfrak{G}}=\dot{\mathfrak{G}}(\mathfrak{A},\mathfrak{C}),\quad \dot{\mathfrak{G}}_1(\mathfrak{F},\mathfrak{C}),\quad [\dot{\mathfrak{G}}_2,\mathfrak{G}](\mathfrak{F},\mathfrak{G}),\quad \dot{\mathfrak{G}}_3(\mathfrak{F},\mathfrak{G}),\quad \dot{\mathfrak{G}}_3(\mathfrak{$$

Vyanjana, Consonants: உயிர்-மெய்எழுத்து (अवर्गाक्षर) $\dot{\mathbf{u}}$ (स्, у), ர் (र्, r), ல் (ल्, l), வ் (व्, v), $\dot{\mathbf{v}}$ (श्, S), ஷ் (ष्, Sh), ஸ் (स्, s), ஹ் (ह्, h) ள் (ळ्, L). [ழ் (zh), ,ற் and ன் (न्)] are special scripts for Tamizh only. [க்ஷ and ஸ்ரீ] are gunitakshara (गुणिताक्षर) in *Devnagari*.

Introduction: -

Base ten place-value system having ten digits from 1 to 9 and 0 for number reckoning is the universally acclaimed invention by the visionaries of ancient India. Since then, numerals of numbers were written using the rule

Purport: - The digits (in the numeral of a number) move '(increase) towards left (in multiples of the base)'.

Cryptic numerals using words and alphabets were popular in Sanskrit texts to denote numbers in rhythmic slokas for easy memorization.

Arvabhata-I (5th c. AD) has named the names of nine place values, thus;

Purport: - The ten names in the multiples of 10 are; एकं(10^{0}), दशं(10^{1}), शतं(10^{2}), सहस्रं(10^{3}) अयुतं(10^{4}), नियुतं(10^{5}), प्रयुतं(10^{6}), कोटि(10^{7}), अर्बुदं(10^{8}), वृन्दं(10^{9}).

Aryabhata-I invented a unique cryptic numerical system adapting Devnagari alphabets to denote the astronomical numbers for the number of revolutions of Geo-centric planets in a Mahayuga (43,20,000 yrs). It is really surprising that these Aryabhatiya Cryptic numerals on conversion into their sidereal periods (time taken to go round ones in their orbits) almost agree with their present-day values.

A. De-coding *Aryabhatiya Cryptic Numerals*, and its application to Modified Tamizh Script.

1. Rule for Aryabhatiya Devanagari Varnamala Cryptic Numerals: -

वर्गाक्षराणि वर्गेऽवर्गेऽवर्गाक्षराणी कात् इमौ यः।

खद्विनवके स्वरा नव वर्गेऽवर्गे नवान्त्यवर्गे वा ॥

வர்கா₂க்ஷராணி வர்கே₂sவர்கே₂sவர்கா₂க்ஷராணி காத் ங்மௌ யஃ |க₁த்₂விநவகே ஸ்வரா நவ வர்கே₂sவர்கே₂ நவாந்த்ய வர்கே₂ வா || Purport: -

- (1) Consonant, व्यञ्जन (மெய் எழுத்து) (a) वर्गाक्षर (மெய்எழுத்து) from क् (க்) [(to म् (ம்)] has numerical value from 1 (to 25) and (b)अवर्गाक्षर, (உயிர்மைஎழுத்து) from ய் [(to (ஹ்)] has numerical value from 3 (to 10) to denote numbers.
- (2) Vowels, स्वराक्षर अ, इ, उ, ऋ, लू, ए, ओ, ऐ, औ; (உயிர் எழுத்து; அ, இ, உ, று. ல்று, ஏ, ஓ, ஐ, ஒள) specify two sets of nine zeros (in multiples of 10), (i) One set of nine even number of ten-zeros to follow वर्गाक्षर (மெய்எழுத்து) and (ii) Another set of nine odd number of ten-zeros to follow मूल-अवर्गाक्षर ((உயிர் மெய்எழுத்து)).

The meaning of the rule could be explained thus with Tables: -

A 1 (1) Consonant, व्यञ्जन (a) वर्गाक्षर (மெய்எழுத்து) from क् (க்) [(to म् (ம்)] has numerical value from 1 (to 25) and (b)अवर्गाक्षर, (உயிர்மைஎழுத்து) from ய் [(to (ஹ்)] has numerical value from 3 (to 10) to denote numbers.

वर्गाक्षराणि वर्गे कात डमौ यः।

वर्गाक्षराणि वर्गे कात् । means $\overline{\Phi} = 1 = (\overline{\Phi} \cdot \mathcal{A}) = (1 \cdot \mathcal{A}); \ \overline{\Phi} = 1$, $[\mathcal{A} = 1]$ Hence the numerical value of वर्गाक्षर $\overline{\Phi} = 1$, $[\mathcal{A} = 1]$.

अवर्गाक्षराणि अवर्गे ङ्गौ यः ।

अवर्गाक्षराणि अवर्गे ङ्गौ यः । means ङ्ग = य

$$\overline{\S}' = [(\overline{\S}' + \overline{\P}) \times \overline{\S}] = [(5+25) \times 1] = [30] = (3\times10)$$

$$= \mathbf{u} = (\mathbf{u} \times \mathbf{u}) = (3 \times 10) = 30 ; [\mathbf{u} = 10].$$

Hence the numerical value of अवगक्षिर $\overline{\mathbf{q}} = 3$, [$\mathbf{3} = 10$].

- A 1 (1) (a) वर्गाक्षर (மெய்எழுத்து) from क् (க்) has numerical value from 1 (to 25); Numerical values of वर्गाक्षर (மெய்-எழுத்து) starts with क् = 1 (க் = 1).
 - (1) (a). (i) वर्गाक्षर (மெய்எழுத்து) from क् (க்) to ज् (ஞ்) denotes numbers from 1 to 10 in order.

Table (1) (a) (i)

Cryptic Numeral for வர்காக்ஷர (மெய்யெழுத்து) from क् (க்) to ञ् (ஞ்)										
Time New Roman Numerals	1	2	3	4	5	6	7	8	9	10
Time New Roman Cryptic Numerals	k	K	g	G	~g	С	С	j	J	~j
वर्गाक्षर (Nirmala UI)	क्	ख्	ग्	घ्	ङ्	च्	छ्	ज्	झ्	ন্
மெய்யெழுத்து	க்	க் ₁	க் ₂	.	脑	ச்	ச் ₁	ச் 2	ச் ₃	ஞ்

(1) (a) (ii). वर्गाक्षर (மெய்எழுத்து) from ट् (ட்)) to म् (ம்) denote numbers from 11 to 25 in order.

Table (1) (*a*) (ii)

			Cr	yptic N	Numera	al from	L=1	1 to in	= 25						
Numbers	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25
Cryptic Numerals	T	Th	D	Dh	N	t	th	d	dh	n	p	P	ь	В	m
वर्गीक्षर (Nirmala UI)	ट्	ą	इ	द	ण्	त्	થ્	द्	ध्	न्	ų	फ्	ब्	મ્	म्
மெய்எழுத்து	Ĺ	Ė ₁	Ŀ ₂	Ŀ ₃	60 <u>0</u> 1	த்	த் ₁	த் ₂	த் ₃	6ðT	Ú	Ú ₁	ப்2	<u>і</u> з	ம்

(1) (b) अवर्गाक्षर, (உயிர்மைஎழுத்து) from ய் [(to (ஹ்)] denote numbers from 3 (to 10) in order.

मूल अवर्गाक्षर (உயிர் மைஎழுத்து) from य् (ய்) to ह् (ஹ்) denote numbers from 3 to 10 sequentially.

Table I (b)

Cryptic Numeral for अवर्गाक्षर (உயிர்மையெழுத்து) from य् to ह् (from ய to ஹ்)								
Numbers	3	4	5	6	7	8	9	10
Cryptic Numerals	у	r	1	v	S	Sh	s	h
वर्गाक्षर (Mangal)	य्	र्	ત્	व्	श्	ष्	स्	ह
உயிர்மையெழுத்து	ய்	Ţ	ல்	வ்	บับ	छंद	ஸ்	ஹ்

Numerical value for vowel स्वरा अ = 1 regarding वर्गीक्षर (மெய்எழுத்து),

Numerical value for vowel स्वरा अ = 10 regarding अवर्गाक्षर (உயிர் மெய்எழுத்து). Hence, the rule (2).

- (2) Vowels, स्वरा अ, इ, उ, ऋ, लू, ए, ओ, ऐ, औ; (உயிர் எழுத்து; அ, இ, உ, று. ல்று, ஏ, ஓ, ஐ, ஔ) specify two sets of nine zeros (in multiples of 10).
- (i) One set of nine even numbers of ten zeros to follow वर्गाक्षर (மெய்எழுத்து).
- (ii) Another set of nine *odd numbers of ten zeros* to follow अवर्गाक्षर (உயிர் மெய்எழுத்து)

Table (2) (i) & (ii)

Number of zeros to follow (மையெழுத்து உயிர்மையெழுத்து									
Vowels of Devnagari	a	i	u	Ru	lRu	Е	0	ai	au
स्वराक्षर	3T	इ	3	ऋ	ૡૃ	Ų	ओ	Ų	औ
உயிரெழுத்து	அ	a	உ	று	ல்று	ஏ	ஓ	恕	ஔ
Number of zeros to follow மையெழுத்து	0	2	4	6	8	10	12	14	16
Number of zeros to follow உயிர்மையெழுத்து	1	3	5	7	9	11	13	15	17

Modified Rule (2) (i) & (ii): -

- (i) Place-values in powers of ten of the numerals of वर्गाक्षर from क् *to* म् (மையெழுத்து) with vowels स्वर (உயிரெழுத்து) अ is 0 and with स्वर (इ, उ, ऋ, लू, ए, ओ, ऐ, औ; இ, உ, று, ல்று, ஏ, ஓ, ஐ, ஒள) are denoted with one group of nine sets of *even powers of ten* (starting from the index 2 to 16).
- (ii) Place-values in powers of ten of the numerals of अवर्गाक्षर from य् to ह् (உய்ர்மையெழுத்து) with vowels with स्वर (अ, इ, उ, ऋ, लू, ए, ओ, ऐ, औ; அ, இ, உ, று, ல்று, ஏ, ஓ, ஐ, ஒள) are denoted with one group of nine sets of odd powers of ten (starting from the index 1 to 17).

Table for Modified Rule (2) (i) & (ii)

Vowels for Devnagari & Tamizh.	a	i	u	Ru	1Ru	E	0	ai	au
Vowel, स्वर	अ	इ	3	ऋ	નૃ	ए	ओ	Ų	औ
Vowel, உயிரெழுத்து	அ	9	உ	று	ல்று	ஏ	ஓ	සු	ஒஎ
Place-values in powers of ten to each of மையெழுத்து	10°	102	104	106	108	1010	1012	1014	1016
Place-values in powers of ten to each of உயிர்மைஎஉத்து)	101	10 ³	105	107	10 ⁹	1011	1013	1015	1017

लृ is मूलस्वराक्षर in Devnagari. But, it is a गुणिताक्षर too.

[लू = (ल्
$$x$$
ऋ) = (5×10^7) = $5,00,00,000$].

See शशि चयगियिङ्शुकृतः (Ref. page 6 in this paper)

A. 2 Two important Rules illustrated;

Rule 1: When a व्यञ्जन (மை எழுத்து) is connected with a स्वर (உயிர் எழுத்து), it forms a गुणिताक्षर, (உயிர் மைஎழுத்து) and their numerical values are to be multiplied. [Note: गुणित = multiply]

Example:
$$\vec{a} = (\vec{a} \times \vec{s}) = (\vec{a} \times \vec{s}) = (6 \times 1000) = (6 \times 10^3) = 6000.$$

Rule 2: When a व्यञ्जन (மை எழுத்து) is connected with another व्यञ्जन (மை எழுத்து), it forms a संयुक्ताक्षर (உயிர் மை எழுத்து), and their numerical values are to be added. [Note: संयुक्त = add]

Example: सूक्त =
$$[(\underbrace{\pi} \times 5) + (\underbrace{\pi} \times 3) + (\underbrace{\pi} \times 3)]$$

ஸூக்த = $[(\underbrace{\hat{m}} \times 20) + (\underbrace{\hat{b}} \times 2)] + (\underbrace{\hat{b}} \times 2)]$
= $[(9 \times 10^5) + (1 \times 1) + (16 \times 1)]$
= $900000 + 1 + 16 = 900017$

Number of revolutions made by (Geo-centric) Planets in a Yuga (= 43,20,000 years) mentioned in Aryabhatiya through the Devanagari script are only Cryptic.

The same Cryptic words may be Adapted to other language scripts, (for example; in Kannada, Tamizh etc.,), and describe the values of Geo-centric Planers stated in Aryabhatiya of Aryabhata–I (499 AD).

B. 1. Cryptic Devnagari Alphabetical Numerals denoting the Number of revolutions of Geo-centric planets in *Aryabhatiya* of Aryabhata-I (5th c. AD).

Number of revolutions made by (Geo-centric) Planets in a Yuga (= 43,20,000 years) stated above are in the Devanagari script. They are only Cryptic words having no meaning in reality. They could be written in any language script. Now, the above statement in Devanagari script is written in Modified Tamizh Scripts.

Modified Tamizh Script: -

யுக₂ரவிப₃க₂ணா: க்₁யுக்₃று, ஶஶ்ரி சயகி₂யிங்கு₂ஶஶுச்₁றுல்று ஶ்னி டு₃ங்க்₂விக்₃வ, கு₂ரு க்₁ரிச்யுப₃, குஜ ப₃த்₂லிஜுனுக்₁று, பு₂த₃ ஸுகு₂ஶ்ரித்்₁றுன, ப்று₃கு₂ ஜஷபி₂கு₁ச்று ||

Purport: -

Sun; रवि, ख्युघृ, க்பயுக்3று; = 43,20,000,

Moon; शिश, चयगियिङुशुछृल, , சயகி₂யிஙு∪் ச்₁றுல்று; = 5,77,53,336,

Saturn; शनि ढुङ्विघ्व; ြ₃ங்க்₂விக்₃வ = 1, 46,564,

Jupitor; गुरु, खिच्युभ, कं₁ प्रीசंЩ⊔3 = 3,64,224,

Mars; कुज (मङ्गळ), भिद्लझुनुख्ऋ, ⊔3த்₂60 क्र₃ஹக்₁ற = 22, 96,824,

Mercury; बुध, स्गुशिथन, സൗக്ര₂ഗിத்₁றுன = 1,79,37,020,

Venus; भृगु, जषब्खुङ् , ஜஷபी2கு1ச்1ற = 70,22,388.

These numerical values could be verified by the application of Tables I, and II based on Aryabhatiya Devanagari Varnamala Cryptic Numerals, and these could be adapted to Modified Tamizh Scripts;

B. 2. Expansion of Aryabhatiya Cryptic Numerical in Devanagari & Tamizh: -

Sun; रवि, ख्युघृ, க்1யுக்3ஹு,

ख्युघृ = (ख् **x** 3) + (य् **x** 3) + (घ् **x** ऋ)

$$\dot{\mathbf{a}}_1$$
 \mathbf{u} $\dot{\mathbf{a}}_3$ \mathbf{u} = ($\dot{\mathbf{a}}_1$ **x** \mathbf{u}) + ($\dot{\mathbf{u}}$ **x** \mathbf{u}) + ($\dot{\mathbf{a}}_3$ **x** \mathbf{u})
= (2 x 10⁴) + (3 x 10⁵) + (4 x 10⁶) = 4320000

Moon; शिश, चयगियिङुशुङ्ल, சயகி₂யிங्∪ுச்₁றுல்று; चयगियिङुशुङ्ल,

சயகி₂யிங்கு₂ஶுச்₁றுல்று

$$= (6 \times 10^{0}) + (3 \times 10^{1}) + (3 \times 10^{1}) + (3 \times 10^{2}) + (3 \times 10^{3}) + (5 \times 10^{4}) + (7 \times 10^{5}) + (7 \times 10^{6}) + (5 \times 10^{7})$$

= 57753336

Saturn; रानि, ढुङ्किप्प्व, டு3ा कं के2 விக்3 வ

ढुङ्किष्व = (इ . 3) + (इ . इ) + (व . इ) + (घ् . अ) + (व . अ)
(ு ந்க்2விக்3வ = (
$$\dot{L}_3$$
. உ) + (\dot{B}_3 . இ) + (\dot{B}_3 . இ) + (\dot{B}_3 . அ) + (\dot{B}_3 . அ) + (\dot{B}_3 . அ)
= (14×10^4) + (5×10^2) + (6×10^3) + (4×1) + (6×10)
= 1,46,564.

Jupitor ; गुरु ; खिच्युभ, க்շரிச்யுப₃

खिच्युभ = (ख्. इ) + (र्. इ) + (च्. 3) + (य्. 3) + (भ्. 3)

$$\dot{\mathbf{a}}_1$$
ரிச்ய $\dot{\mathbf{b}}_3$ = ($\dot{\mathbf{a}}_1$. इ) + ($\dot{\mathbf{f}}$. इ) + ($\dot{\mathbf{f}}$. 2) + ($\dot{\mathbf{b}}$. 2) + ($\dot{\mathbf{b}}_3$. 3)
= $(2x10^2)$ + $(4x10^3)$ + $(6x10^4)$ + $(3x10^5)$ + $(24x1)$ = 3,64,224.

$$Mars$$
 ; कुज, मङ्गल , भिद्लझुनुख़ , ப $_3$ த் $_2$ லிசு $_3$ னுக் $_1$ று भिद्लझुनुख़ = (भ् . अ)+ (द् . इ) + (ल् . इ) + (झ् . 3)+ (न् . 3) + (ख् . ऋ) ப $_3$ த் $_2$ லிஜுனுக் $_1$ று = (ப $_3$.அ)+ (த் $_2$.இ) + (ல்.இ)+ (ச் $_3$.உ)+ (ந் .உ)+ (க் $_1$. று) = $(24x1)+(18x10^2)+(5x10^3)+(9x10^4)+(20x10^4)+(2x10^6)$ = $22.96.824$.

Mercury ; बुध , सुगुशिथून, ஸுகு₂மித்₁றுன

स्गुशिथृन = (स् .3) + (ग् .3) + (श् . इ) + (थ् .ऋ) + (न् . अ)
ஸுகு₂णித்₁றுன = (ஸ். உ) + (க்₂.உ) + (ஶ். இ) + (த்₁. று) + (ன். அ)
=
$$(9x \ 10^5) + (3x \ 10^4) + (7x \ 10^3) + (17x \ 10^6) + (20x \ 1)$$

= $1,79,37,020$

Venus ; भ्रुगु, शुक्रः , जषबिखुछृ, ஐஷபி₂கு₁ச்₁று

C. 1. Table showing The number of Revolutions (velocity) of (Geo-centric) *Planets* in *a Yuga* (43,20,000 yrs.) arranged in the increasing order in *Aryabhatiya Cryptic Numerals* and in *International Numerals*.

Table C. 1

	mes of tric planets	Number of of Revolutions in a Mahayuga (43,20,000 yrs)						
English	Devnagari	Devnagari	Modified Tamizh	International				
Saturn	शनि	ढुङ्ग्विघ्व	டு ₃ ங்க் ₂ விக் ₃ வ	1,46,564				
Jupitor	गुरु	ख्रिच्युभ	க் ₁ ரிச்யுப ₃	3,64,224				
Mars	कुज, मङ्गळ	भद्तिझुनुखृ	ப₃த்₂லிசு₃ நுக்₁று	22, 96,824				
Sun (Earth)	रवि [भुवि]	ख्युघृ	க் ₁ யு க் ₃ று	43,20,000				
Venus	शुक्र	जषबिखुकृ	ஜஷபி ₂ கு ₁ ச் ₂ று	70,22,388				
Mercury	बुध	सुगुशिथृन	ஸுக்₂மித்₁றுந	1,79,37,020				
Moon	सोम	चयगियिङुशुकृतृ	சயகி யிஙுமுச் றுல்று	5,77,53,336				

C. 2. Comparison of Sidereal periods based on Aryabhatiya values of number of revolutions of Geo-centric planets in a Mahayuga (43,20,000 yrs) (5th c AD), with the Present-day Recorded Sidereal periods: -

Table C. 2

Names of Geo-centric planets	And in Interi	rals in Devanagari & Ta national Numerals for the of Geo-centric planets in (43,20,000 yrs)	Comparison: Aryabhatiya Sidereal period with Their Present-day Sidereal periods			
English	Devnagari	Modified Tamizh	International	Aryabhatiya values	Present-day values	
Saturn	ढुङ्ग्विघ्व	டு₃ங்க்₂விக்₃வ	1,46,564	29.48 yrs	29.46 yrs	
Jupitor	ख्रिच्युभ	க்₂ரிச்யுப்₃	3,64,224	11.86 yrs	11.86 yrs	
Mars	भद्तिझुनुखृ	ப₃த்₂லிஜுநுக் ₁று	22, 96,824	687 days	687 days	
Sun (Earth)	ख्युघृ	க் ₁ யு க் ₃ று	43,20,000	365.26 days	365.26 days	
Venus	जषबिखुछ	ஜைபி ₂ கு ₃ ச் ₂ று	70,22,388	224.69 days	224.69 days	
Мегсигу	सुगुशिथृन	ஸுகு₂யித்₁றுந	1,79,37,020	87.97 days	87.97 days	
Moon	चयगियिङुशुकृतृ	சயகி ₂ யிஙுஶுச் ₁ றுல்று	5,77,53,336	27.32 days	27.32 days	

Formulae to convert Aryabhatiya cryptic numerals of the number of revolutions of Geocentric planets to their sidereal periods are;

Sidereal period =
$$\frac{43,20,000}{\text{number of revolutions of the planet}} \text{ years}$$
Sidereal period =
$$\frac{43,20,000}{\text{number of revolutions of the planet}} \times 365.26 \text{ days}$$

Comparison of *Sidereal periods based on Aryabhatiya values of number of revolutions of Geo-centric planets in a Mahayuga* (43,20,000 yrs) (5th c AD), with the *Present-day Recorded Sidereal periods* is really, an astonishing eye-opener about our rich heritage.

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